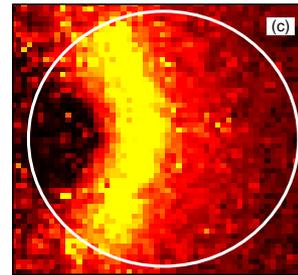
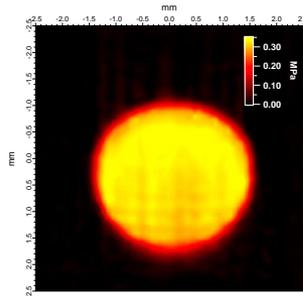


Local friction of rough contact interfaces with rubbers using contact imaging approaches



D.T. Nguyen, M.C. Audry, M. Trejo, C. Fretigny and A. Chateauminois
Soft Matter Science and Engineering Laboratory - SIMM
Ecole Supérieure de Physique et Chimie Industrielles (ESPCI), Paris, France

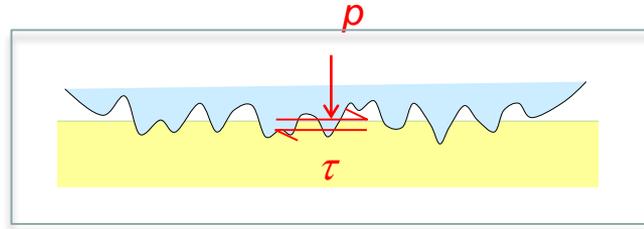


E. Barthel & J. Teisseire
Surface du Verre et Interfaces, CNRS – Saint Gobain, Aubervilliers

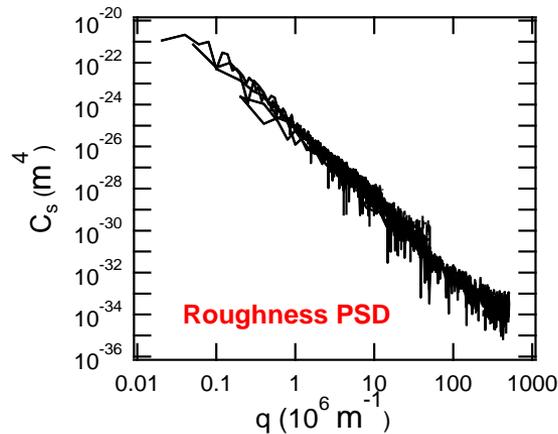


A. Prevost & E. Wandersman
Jean Perrin Laboratory (LJP), Université P. et M. Curie, Paris

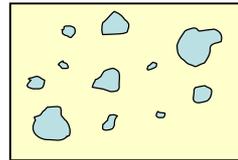
Steady state friction of dry multi-contact interfaces



• Surface geometry, contact mechanics



Micro-contacts distribution



Real contact area ??

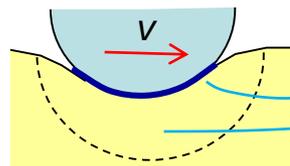
Non linear material response

Adhesion

Viscoelasticity

....

• Frictional energy dissipation at micro-asperity scale



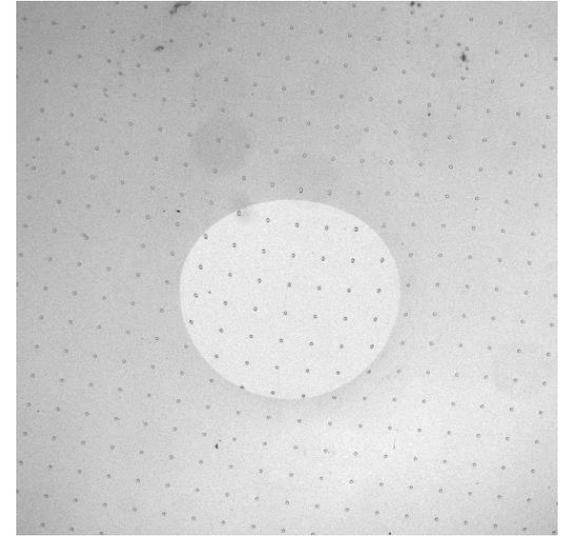
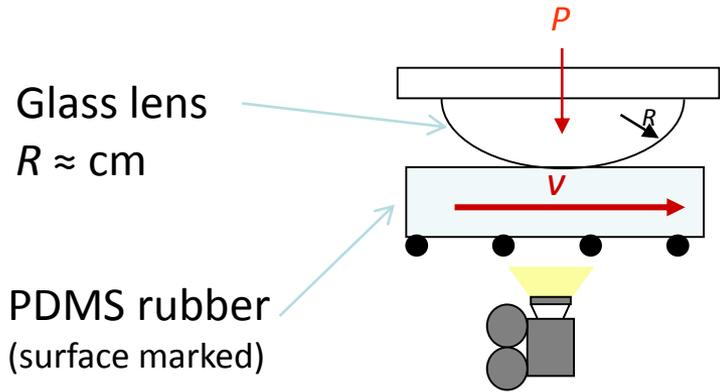
• Interfacial dissipation

• Bulk plastic or viscoelastic dissipation

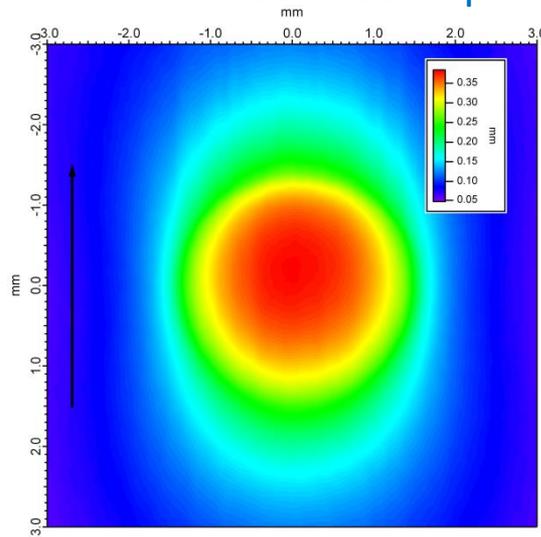


Local friction law $\tau(p)$??

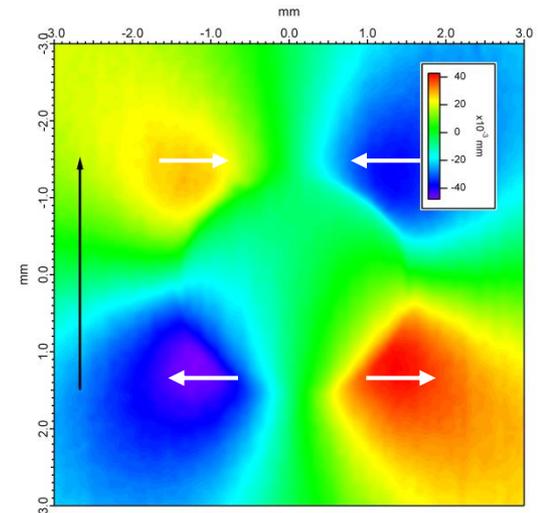
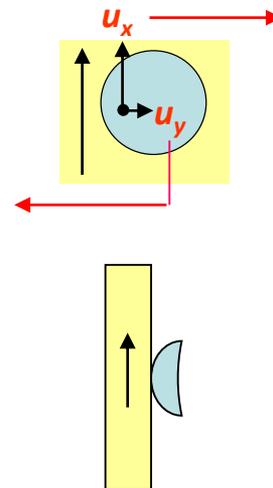
Displacement field measurements within contacts with rubber



Surface displacements during steady state friction



Along sliding direction



Perpendicular to sliding direction

Space resolution $\sim 10 \times 10 \mu\text{m}^2$

Contact stresses : inversion of the displacement field

Inversion???

Surface displacement \rightarrow Surface stresses

- Linear elasticity \rightarrow Green's tensor

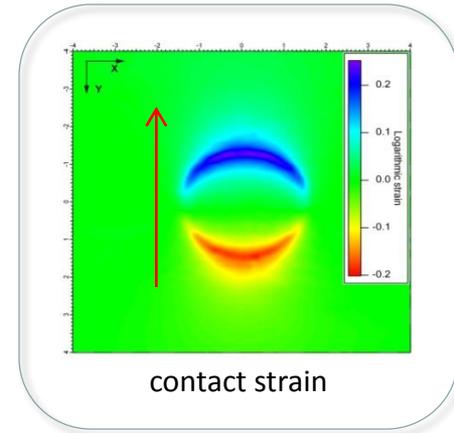
Incompressible materials, $\nu=0.5$

Lateral displacements

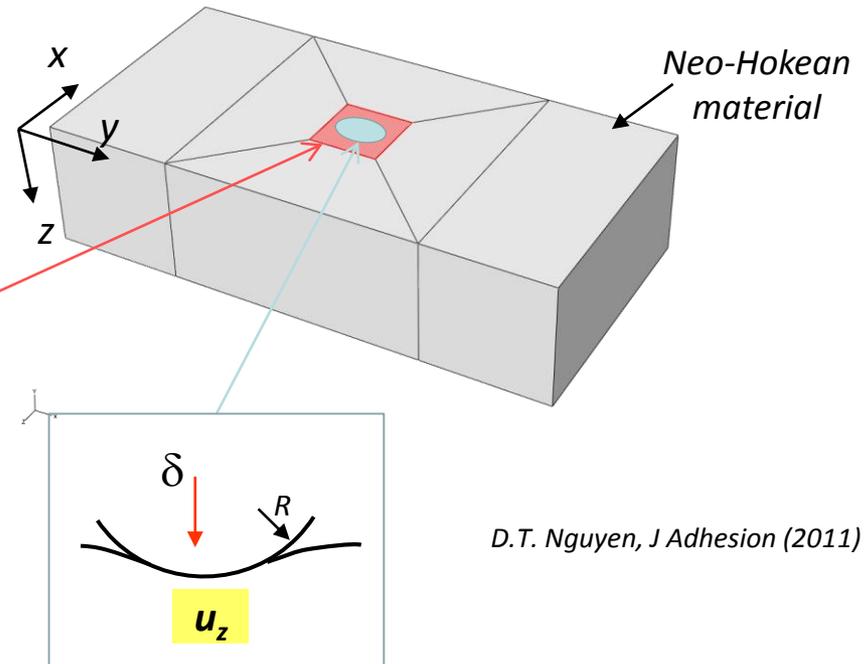
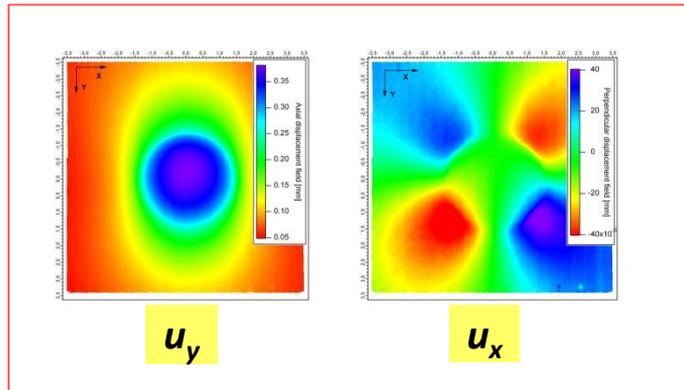
$$u_i = G_{ij} * \sigma_{jz} \quad i, j = x, y$$

Vertical displacement

$$u_{zz} = G_{zz} * \sigma_{zz}$$



- Experimentally : large strains ! \rightarrow Numerical inversion using FEM

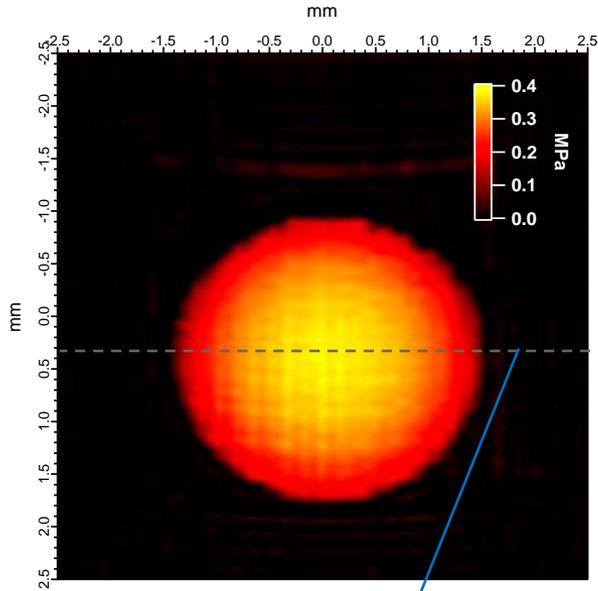


D.T. Nguyen, J Adhesion (2011)

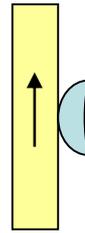
Contact stresses: single asperity contact

Smooth Glass/PDMS contact

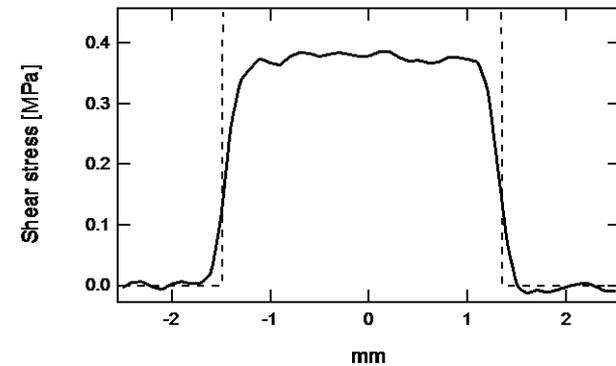
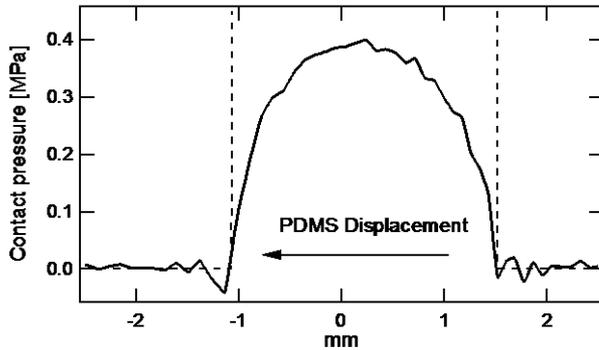
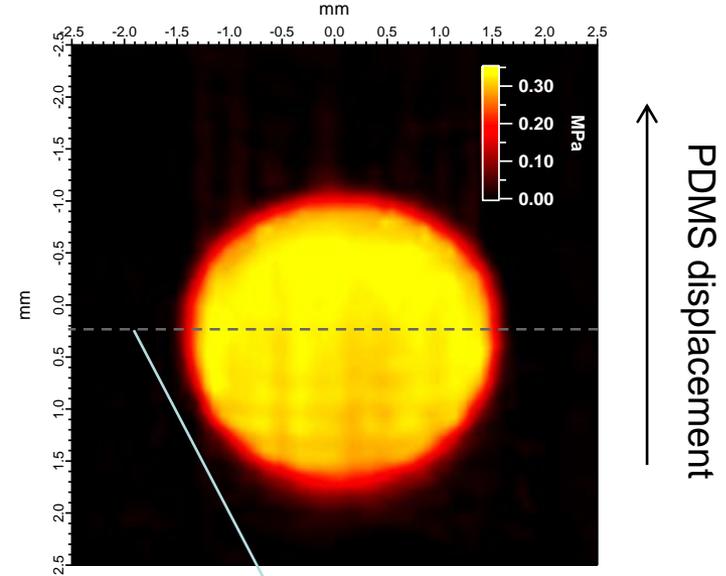
Contact pressure



$R=9.3 \text{ mm}$, $P=1.4 \text{ N}$, $v=0.5 \text{ mm/s}$



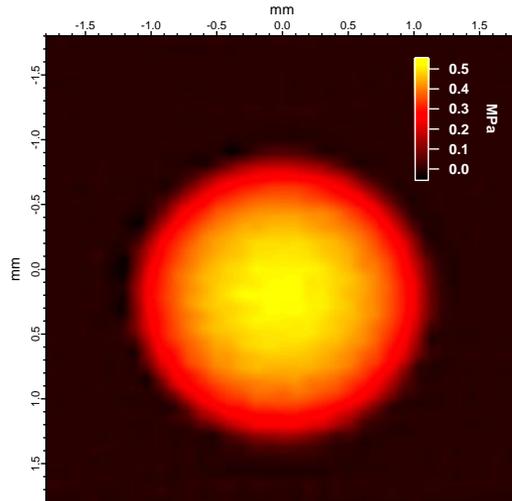
Surface shear stress



Pressure independent shear stress

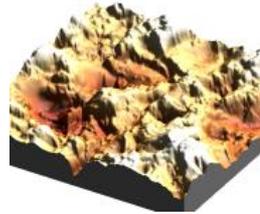
Contact stresses: rough multi-contact interface

Contact pressure



Gaussian roughness

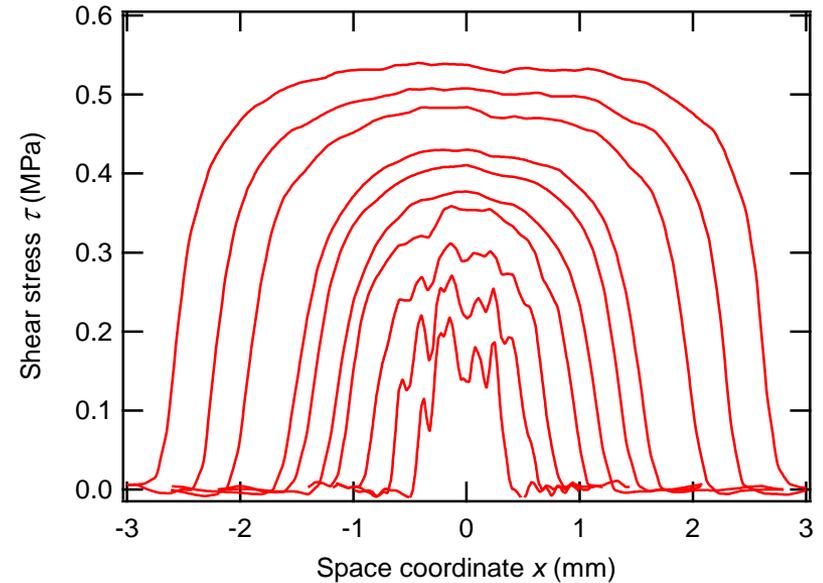
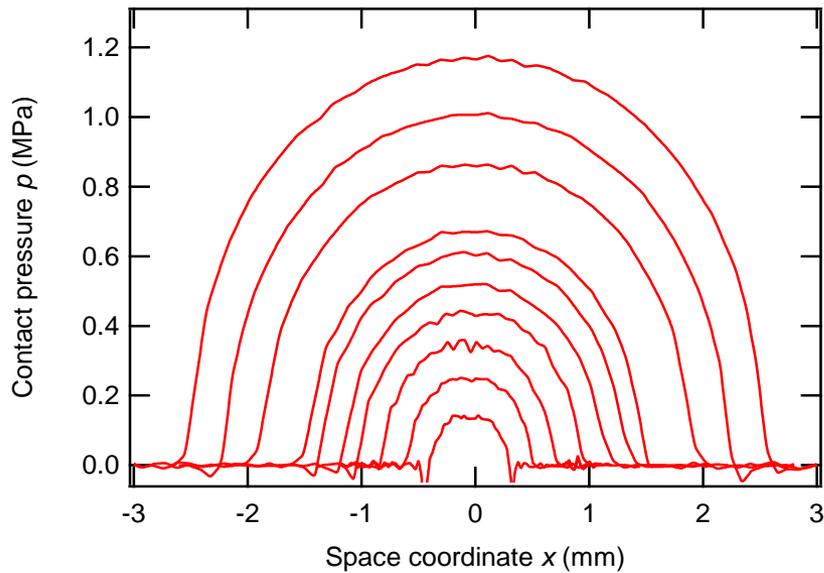
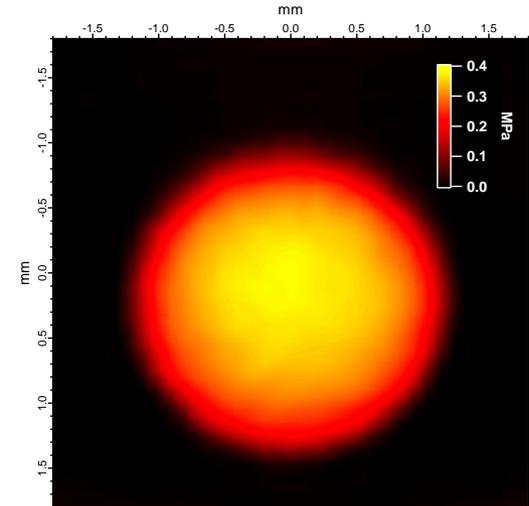
r.m.s roughness $\sim 1 \mu\text{m}$



20 μm

Sand blasted glass lens

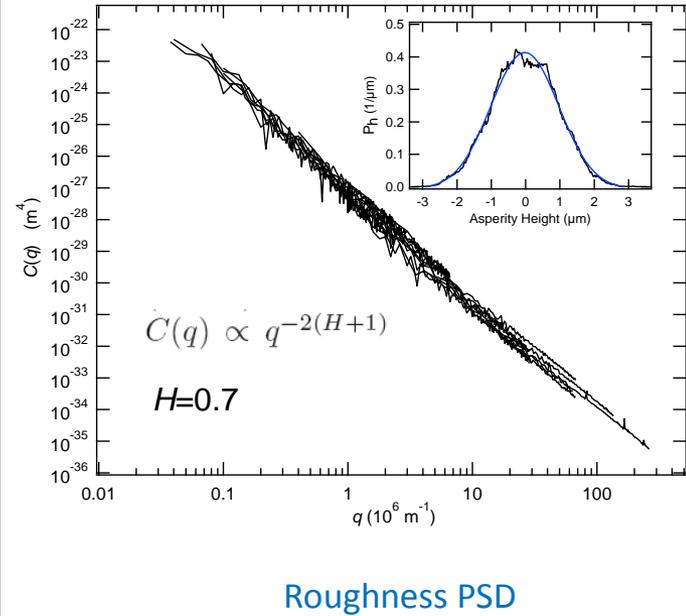
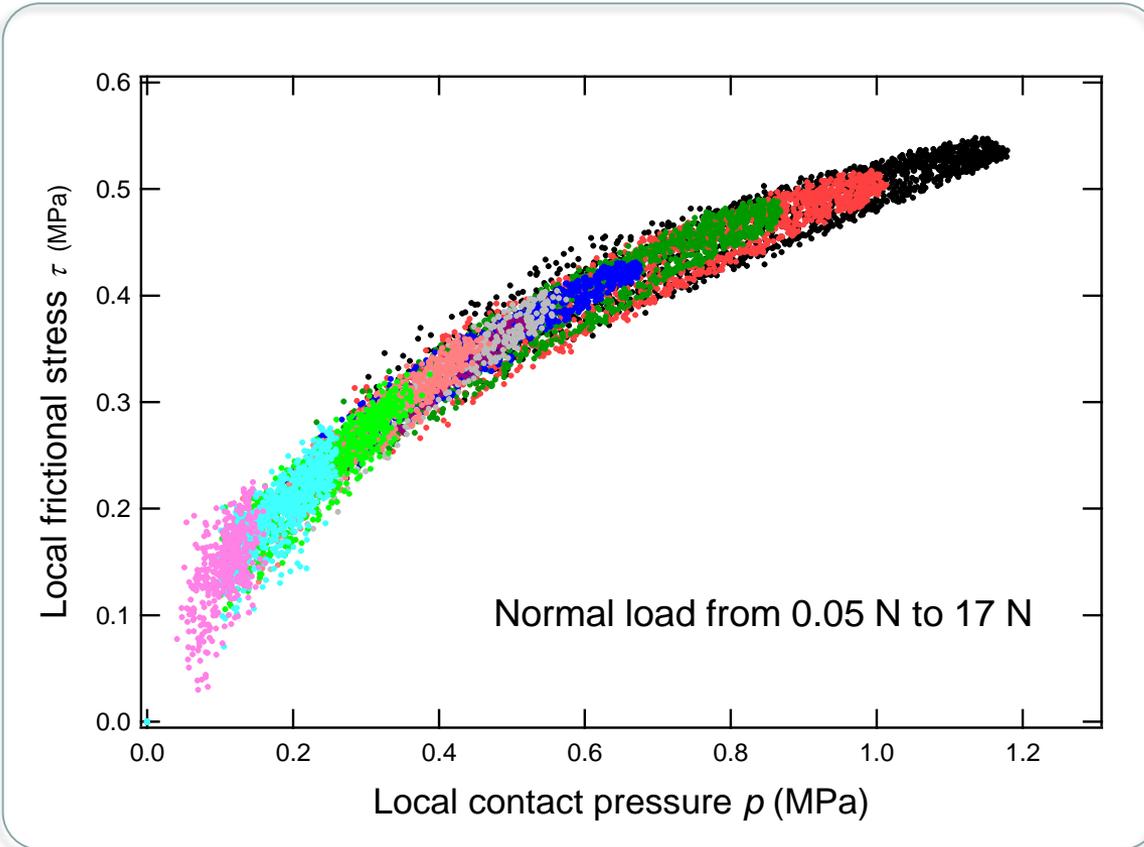
Shear stress



Stress profiles at increasing applied normal load

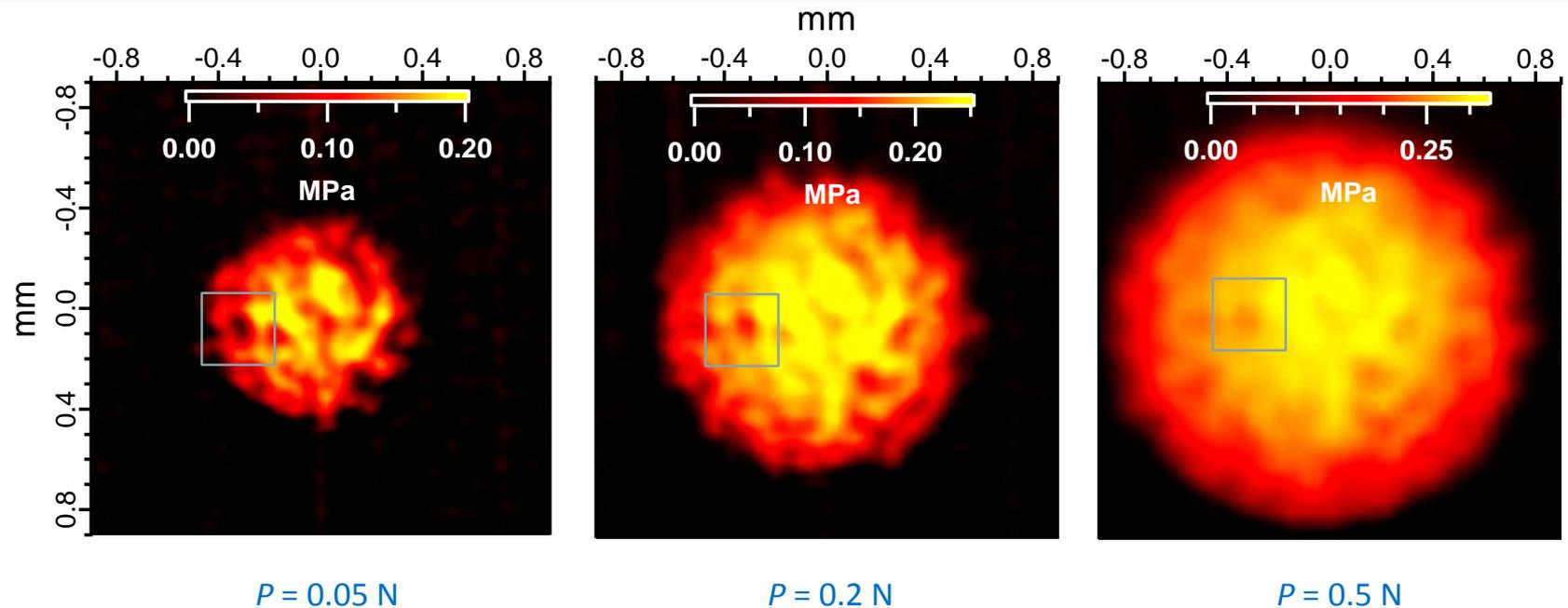
Local friction law

- PDMS / self affine rough glass surface



Non Amontons-Coulomb local friction law

Spatial fluctuations in the shear stress at low contact pressures



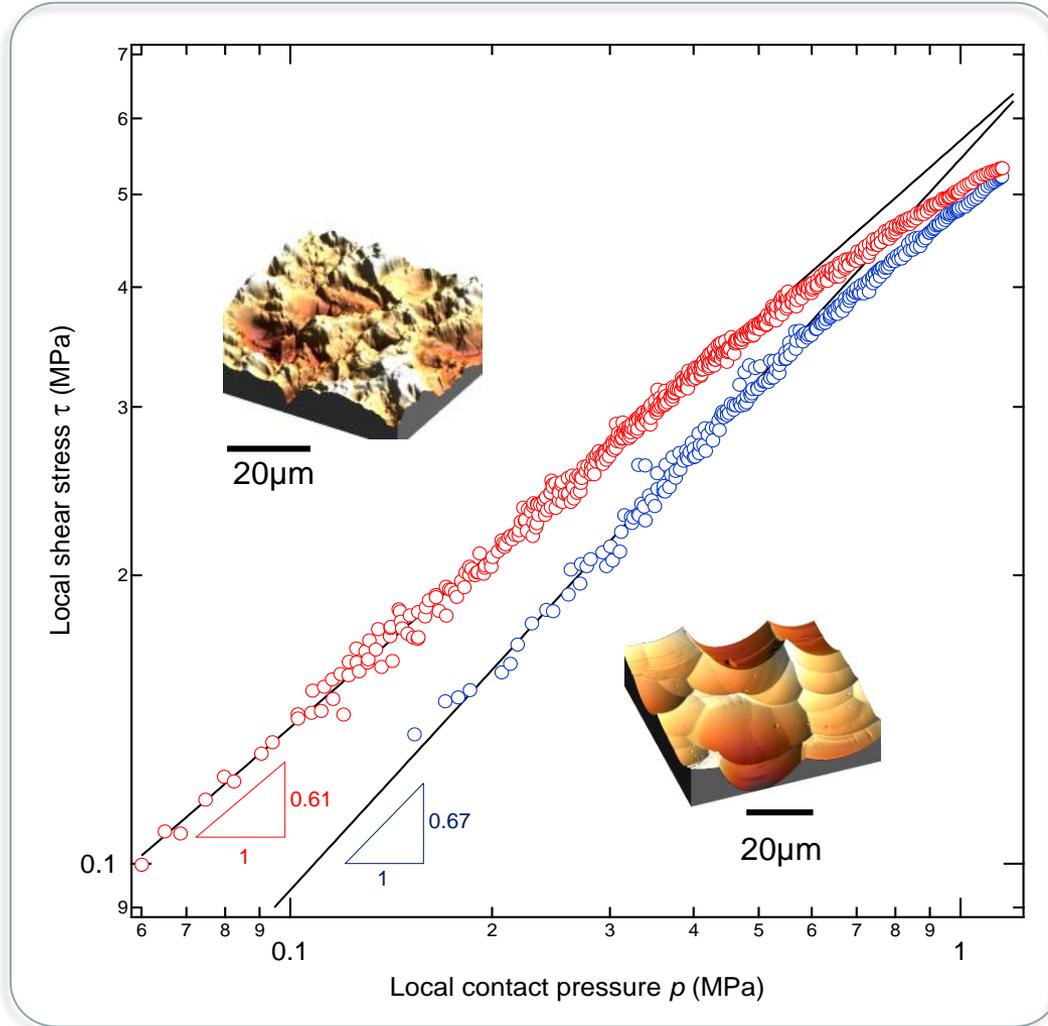
Stress fluctuations over length scales of the order of a few tens of micrometers



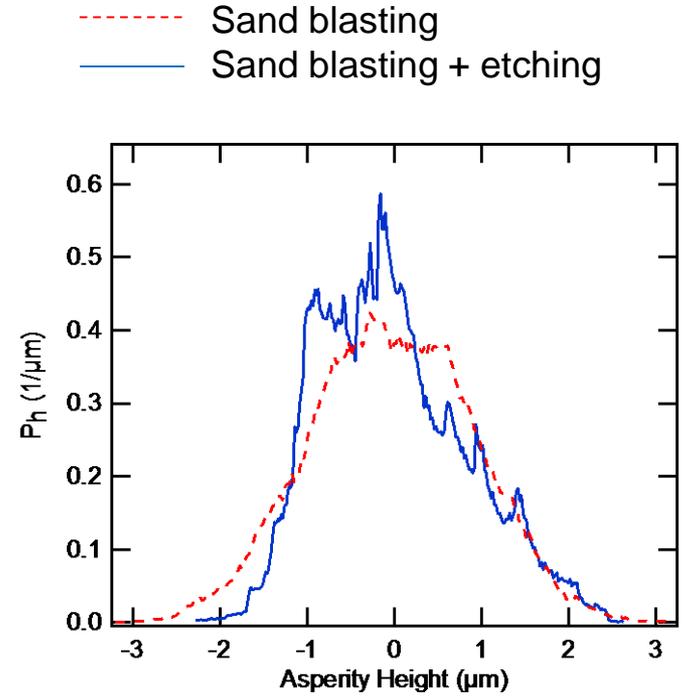
Local changes in the contact stress distribution induced by details of the topography of the rough lens

Gaussian vs non Gaussian surface roughness

- PDMS rubber



Local friction law



Height distribution

Additional roughnesses...

'Cups'



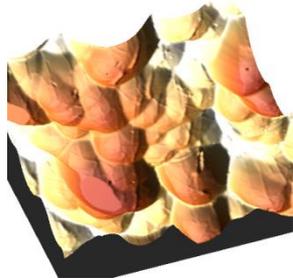
Sol-gel Replica



'Bumps'

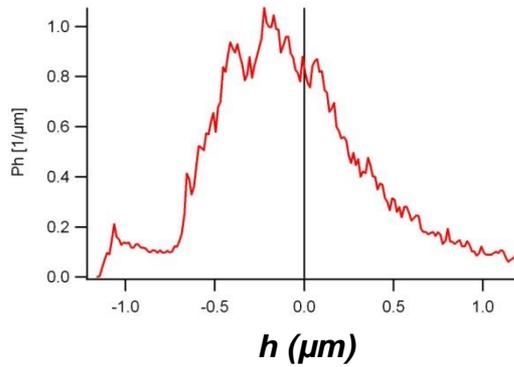


Different height distributions

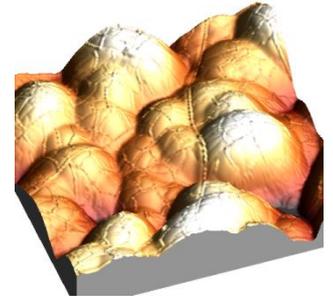
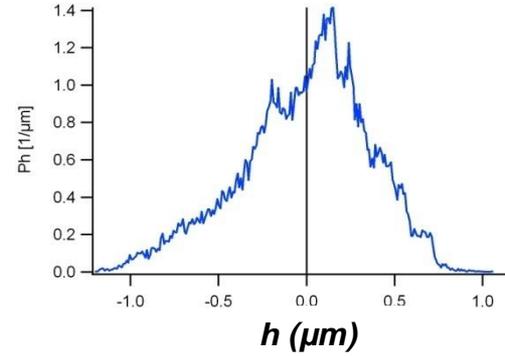


30 μ m

$P_h(1/\mu\text{m})$

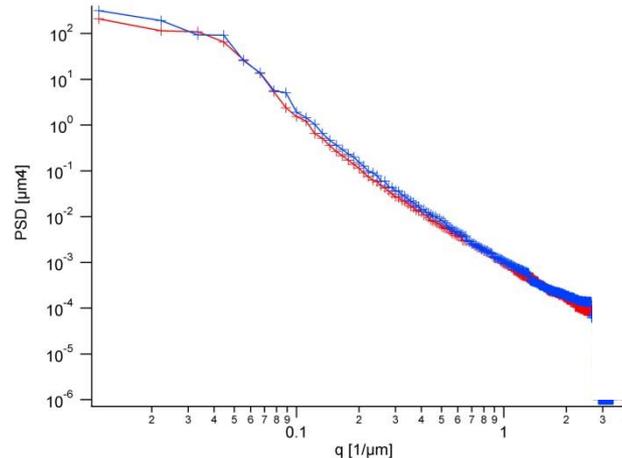


$P_h(1/\mu\text{m})$

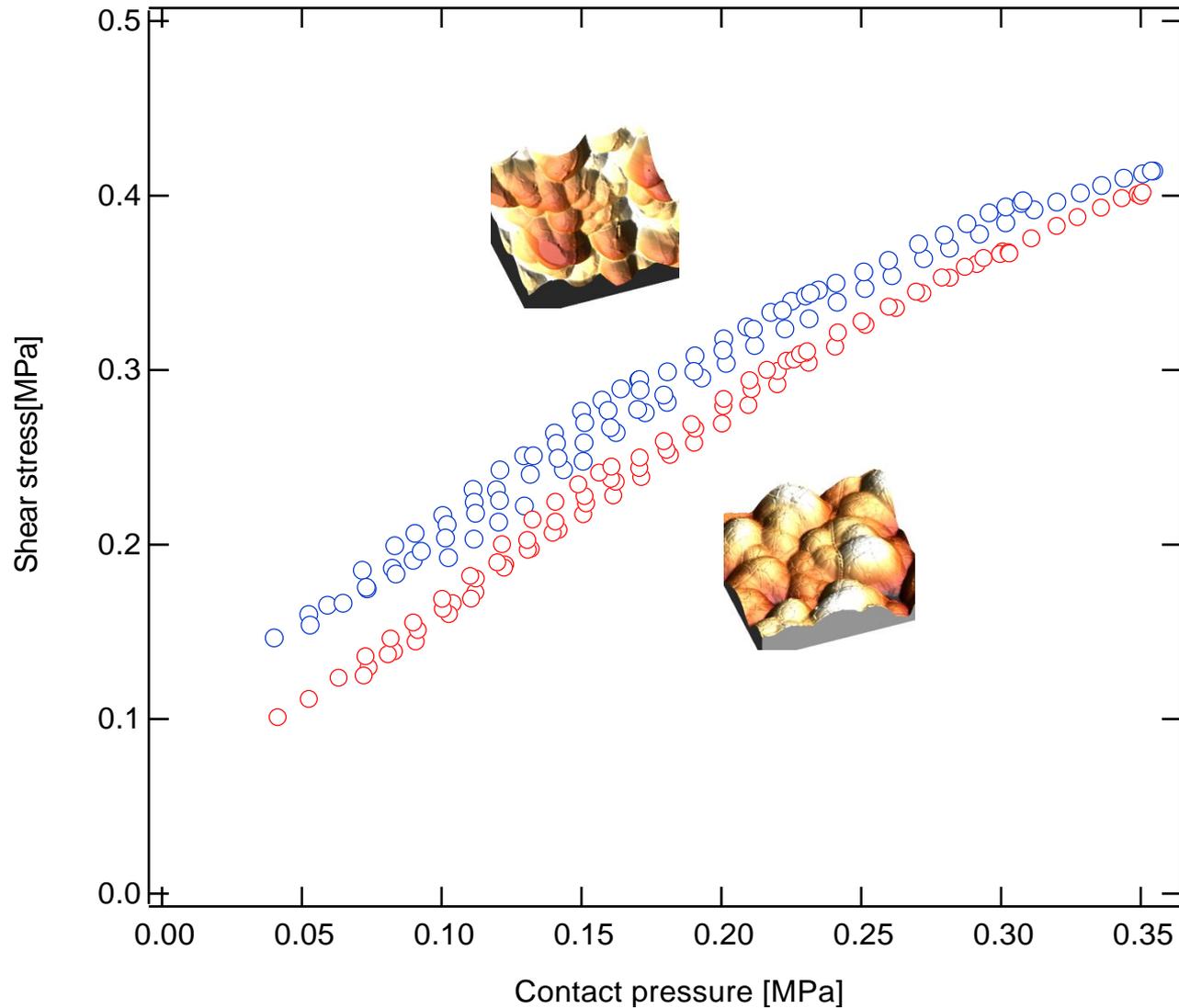


30 μ m

Same roughness power spectrum density

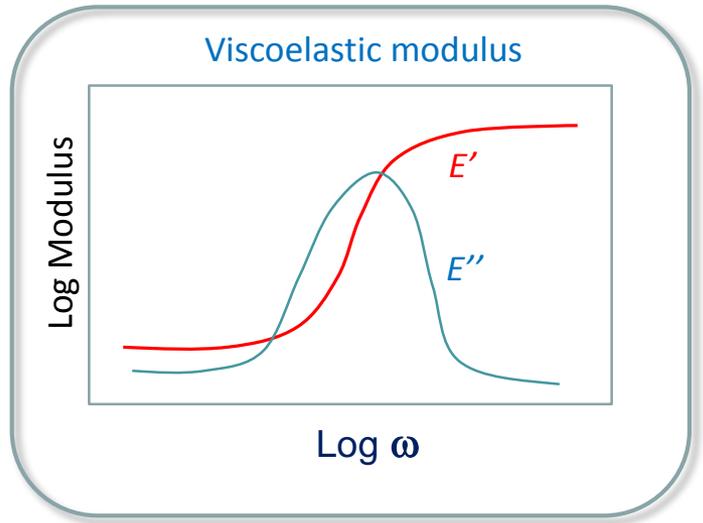
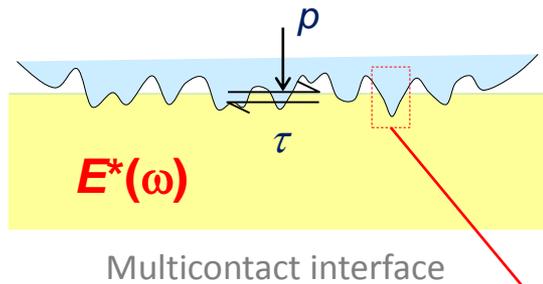


Cusps vs bumps: local friction law

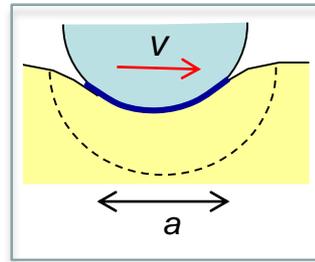


All the topographical information relevant to friction is not embedded in the PSD

Friction of rubbers with rough surfaces: the role of viscoelastic losses



Characteristic frequency $\omega \sim v/a$

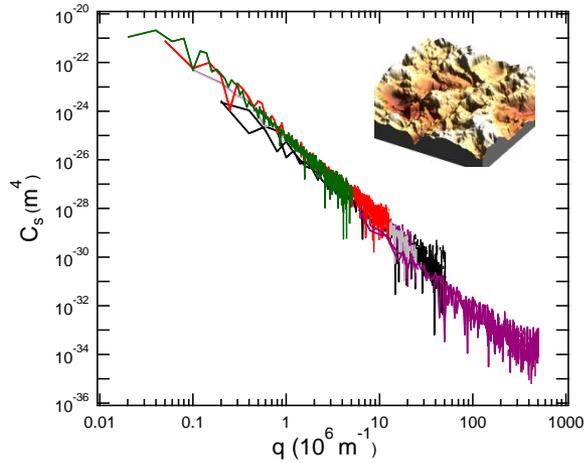


Single asperity contact

- Velocity and pressure dependence of the real contact area ?
- Viscoelastic losses at micro-asperity scale ?

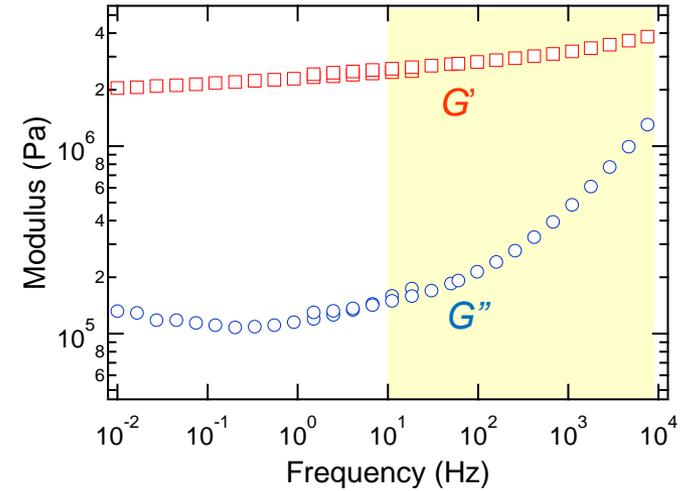
Local friction of viscoelastic rubbers with randomly rough surfaces

Sand blasted glass surface

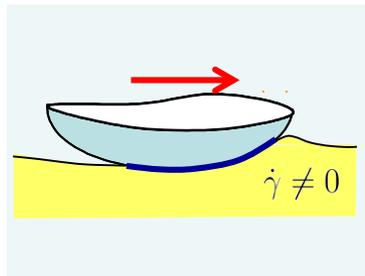


rms roughness \square μm

Epoxy rubber $T_g = -42^\circ\text{C}$

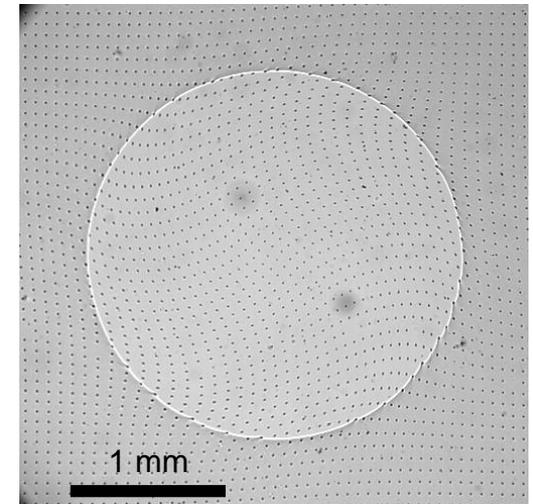
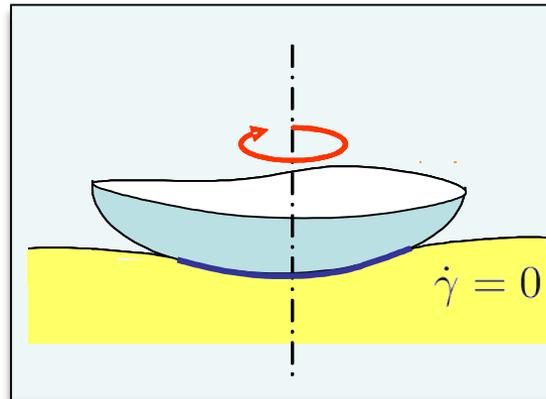


Torsional contacts



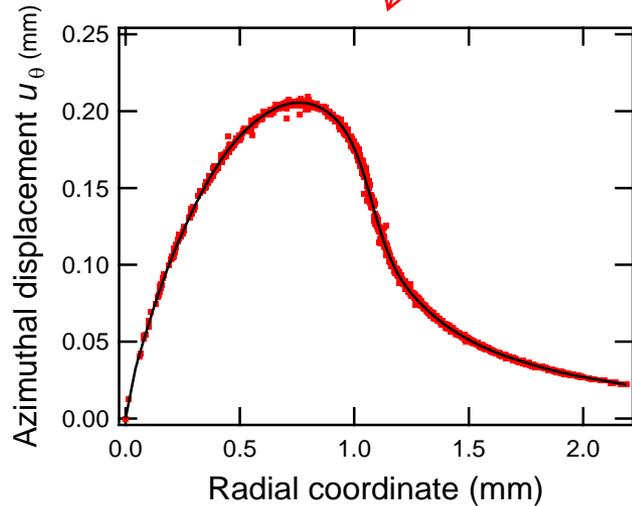
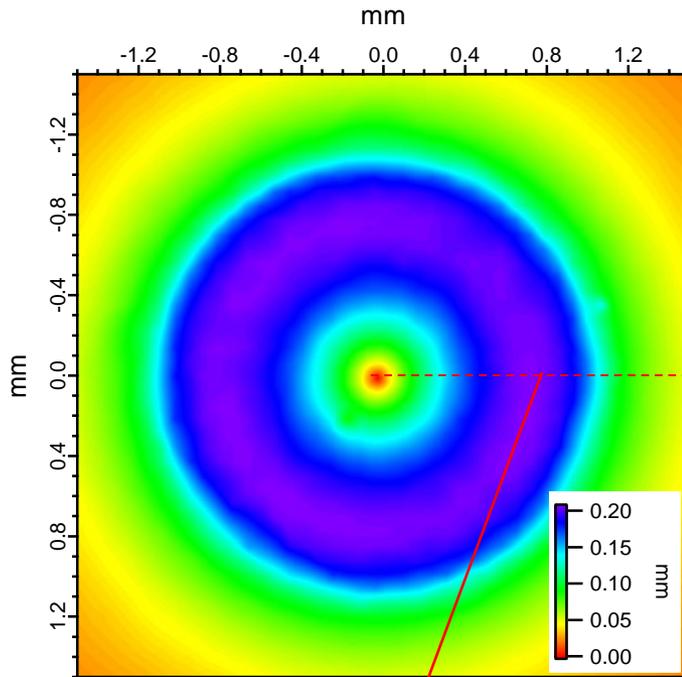
Linear sliding

Bulk viscoelastic dissipation
at contact scale !



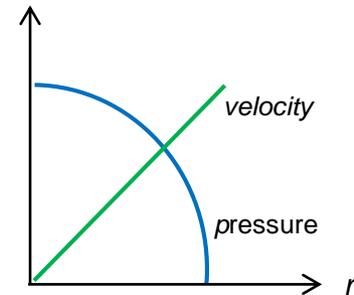
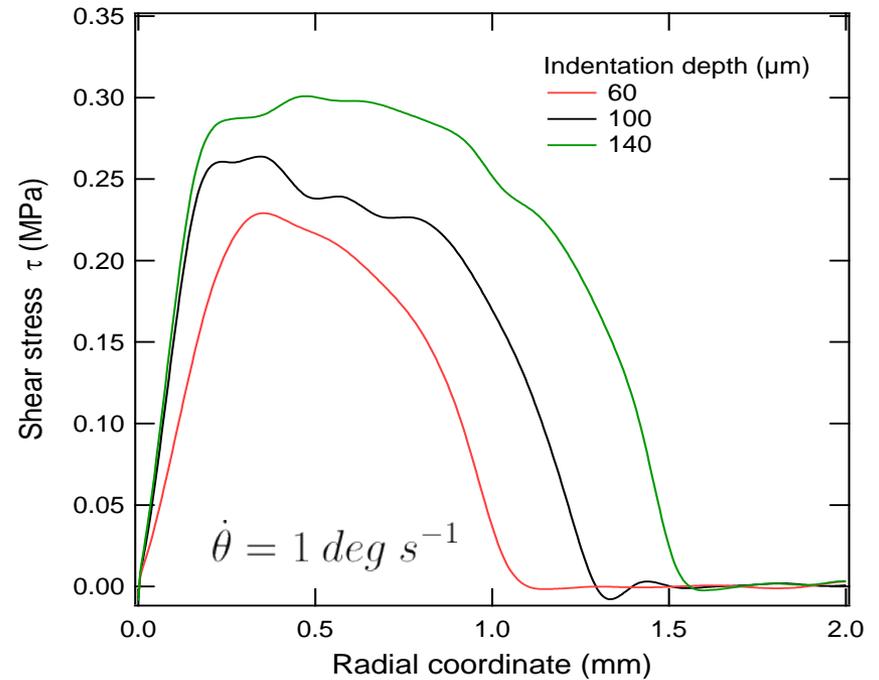
Torsional contact : displacement & stress field

Azimuthal displacement u_θ



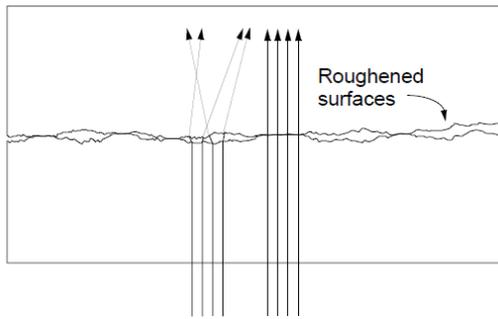
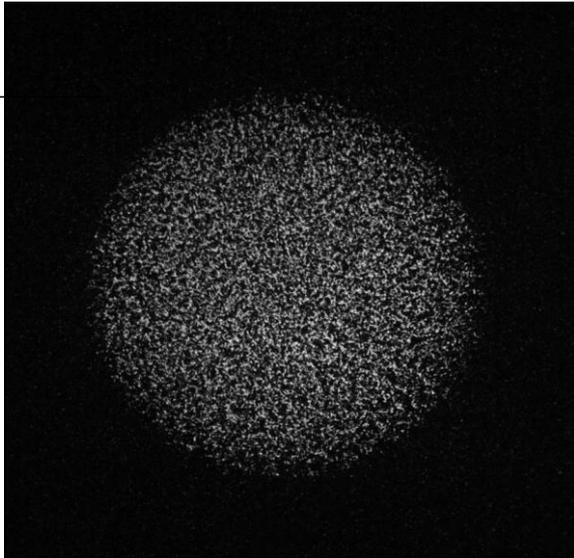
Inversion 

Frictional shear stress



Light transmission through rough multi-contact interfaces

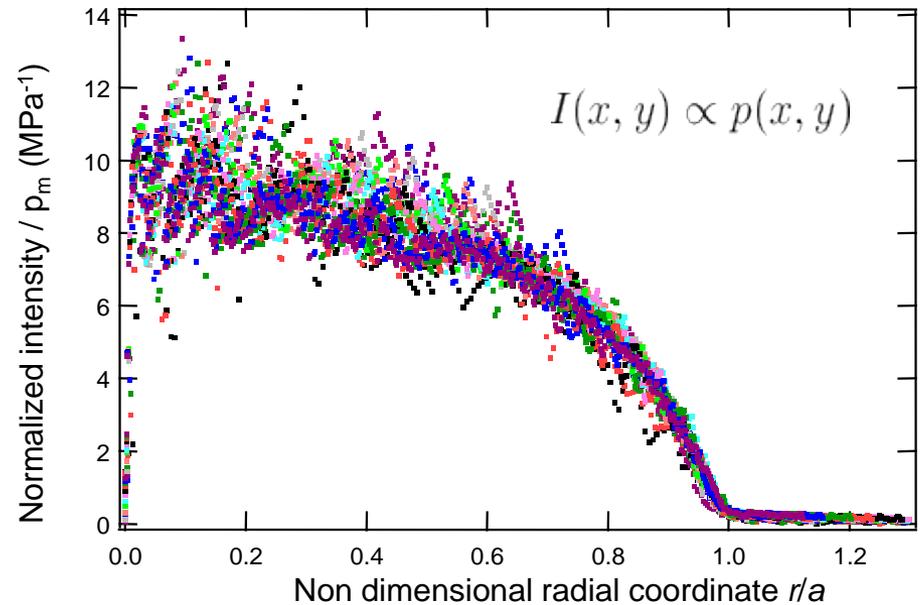
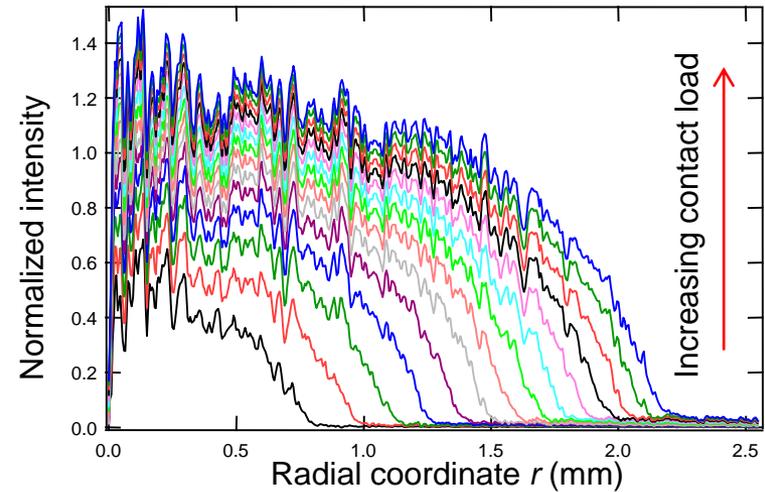
1 pixel = 5.1 μm



Dieterich *et al.* Pageoph, **143** (1994)

Light transmitted through the interface more efficiently when only one interface is present

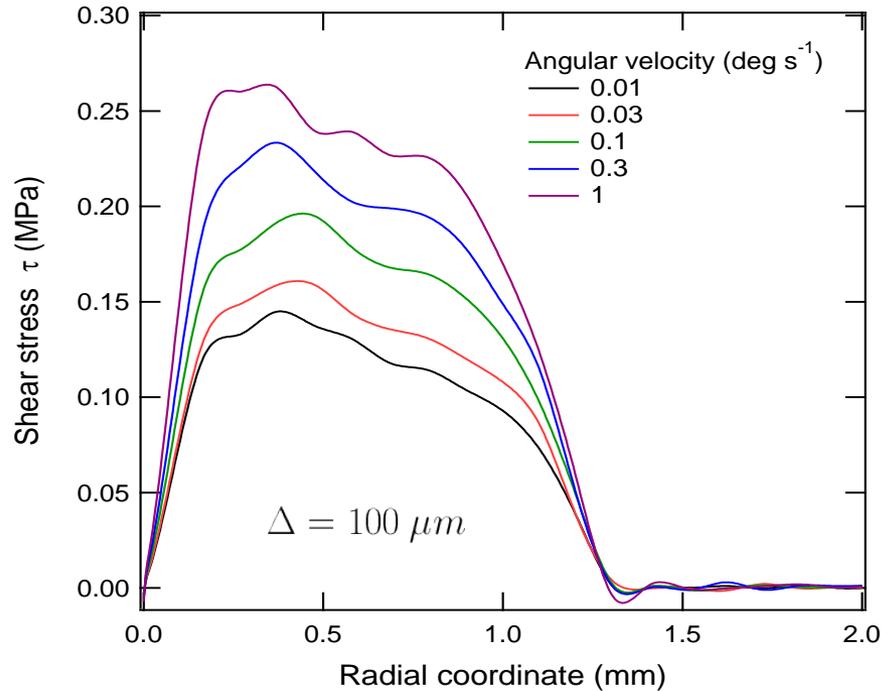
Static indentation experiments



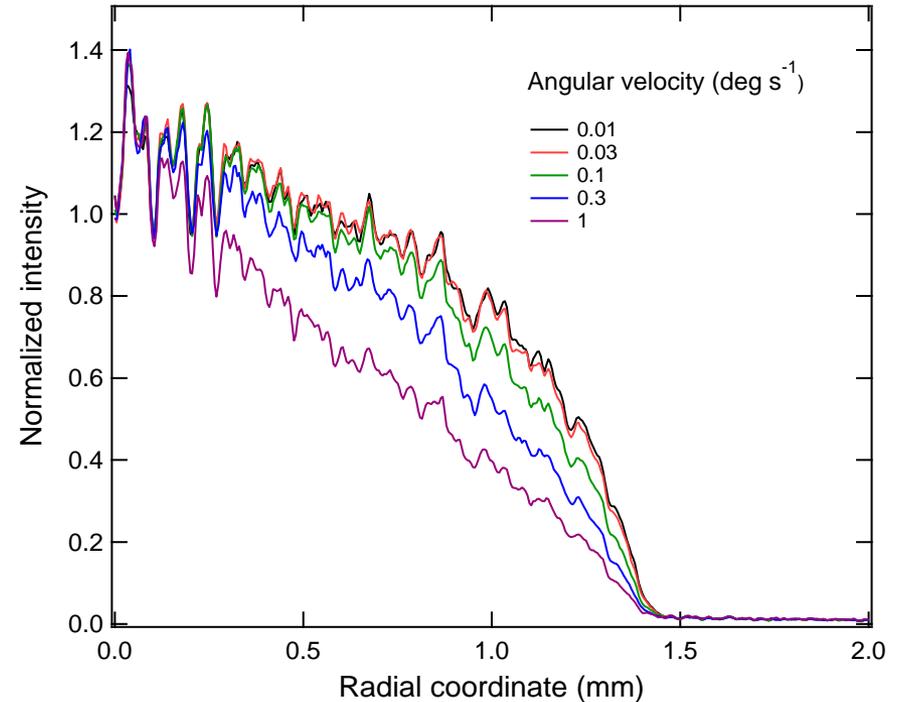
Transmitted light intensity $I(x,y) \propto$ Proportion of area in contact $A/A_0(x,y)$

Velocity dependence of the shear stress

Angular velocity



Transmitted light intensity

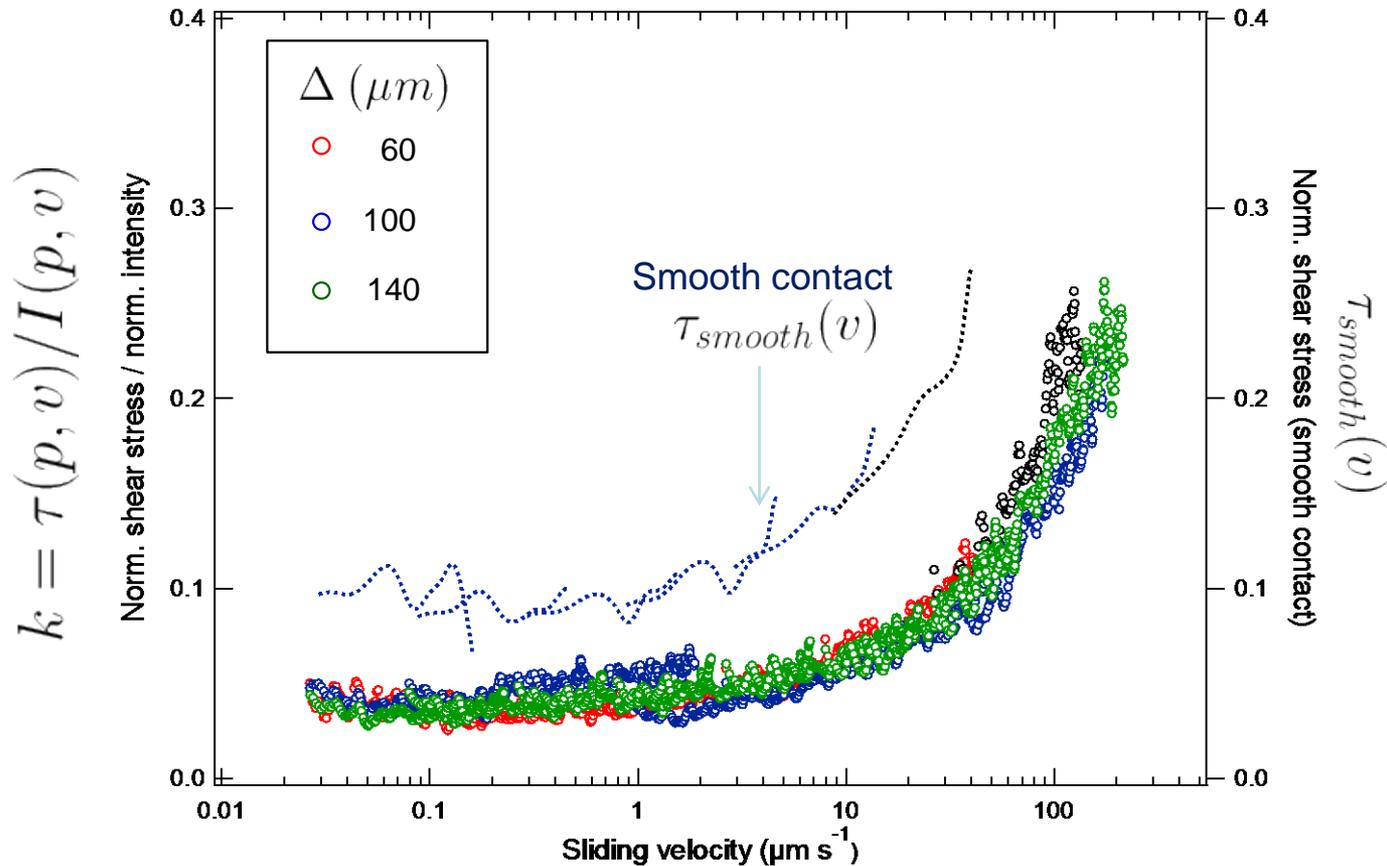


Dependence of the shear stress on the actual contact area :



$$\tau(p, v) / I(p, v) \quad ???$$

Pressure and velocity dependence of the frictional shear stress



$$\tau(p, v) \propto k(v) A / A_0(p, v)$$

Average shear stress within micro-asperity contacts

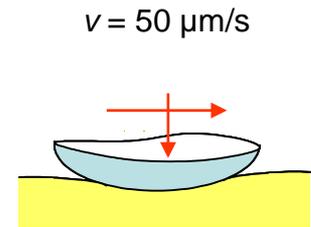
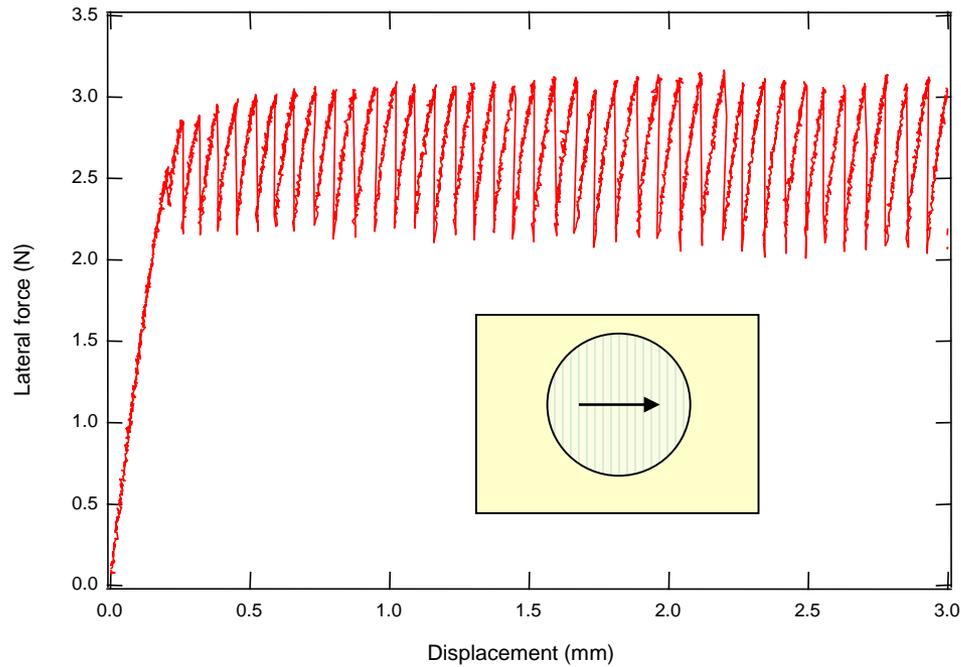
Real contact area: density of micro-contacts

$k(v) \approx \tau_{smooth}(v) \rightarrow$ Interface dissipation predominates over bulk viscoelastic dissipation

Unsteady state friction:

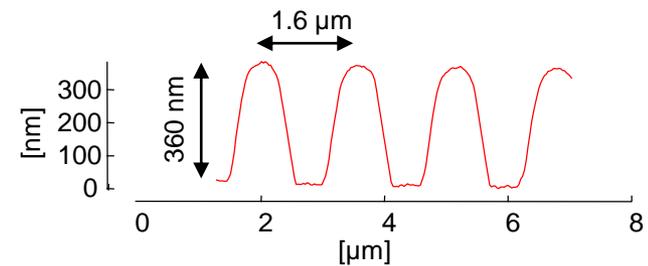
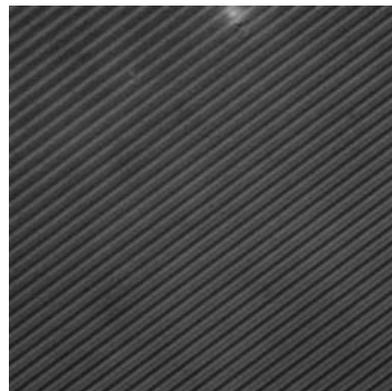
Stick-slip motions within patterned glass/PDMS contacts

Stiction of patterned glass surfaces : stick-slip motions

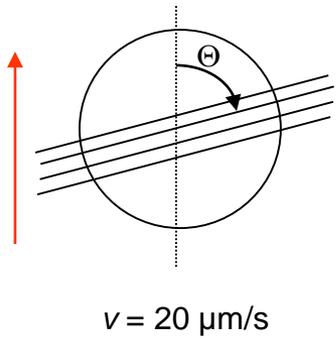


Patterned glass lenses

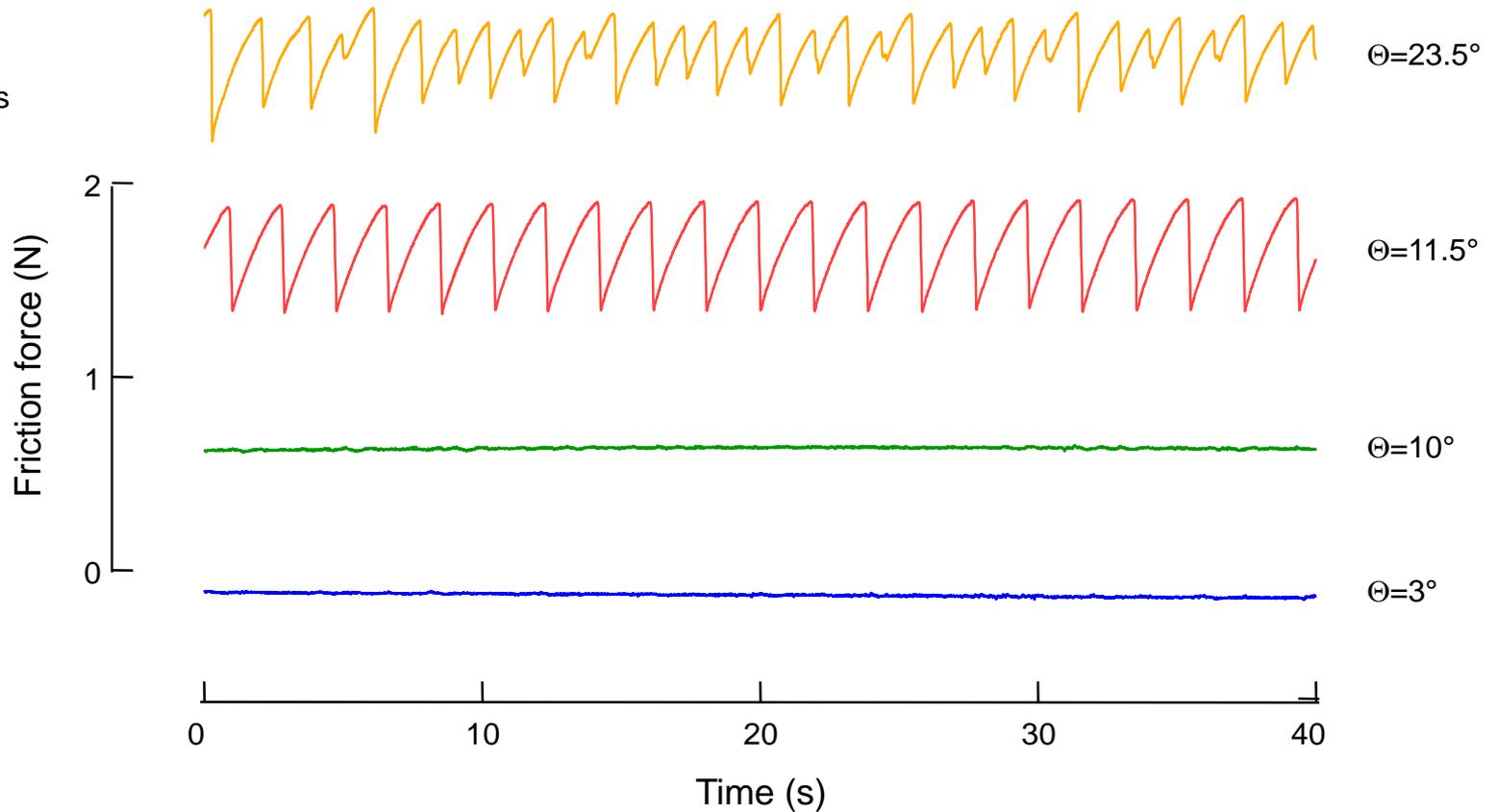
Sol-gel process, Saint Gobain



Friction traces vs ridges orientation

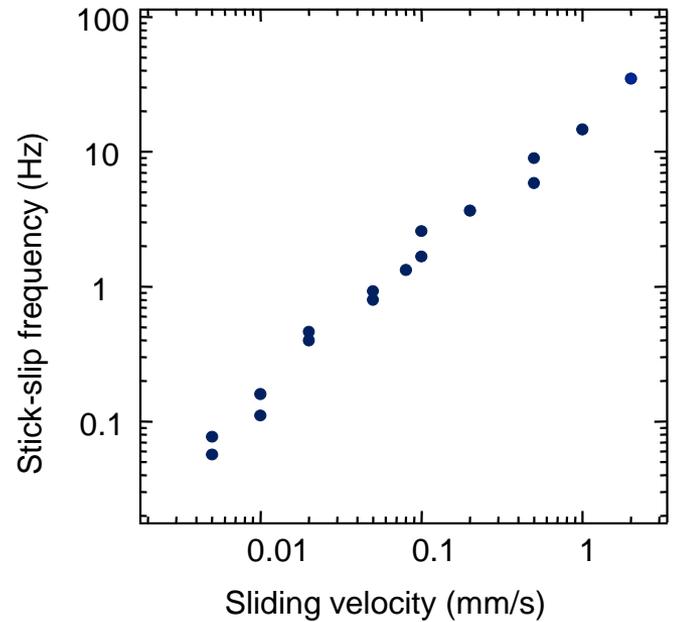
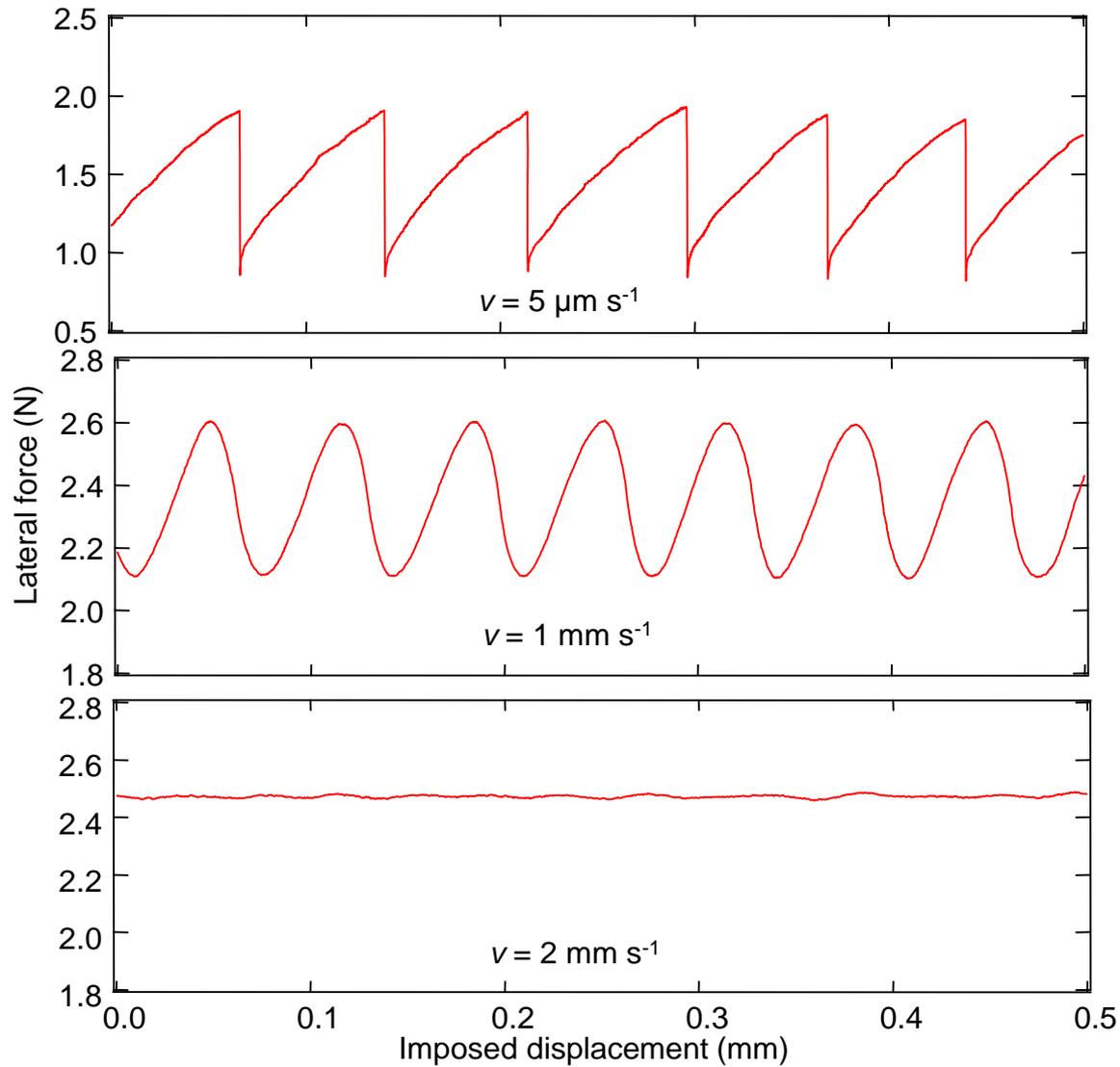


Critical angle for the occurrence of stick slip $\Theta_c \sim 11^\circ$



Stick-slip generated by localized stress fluctuations

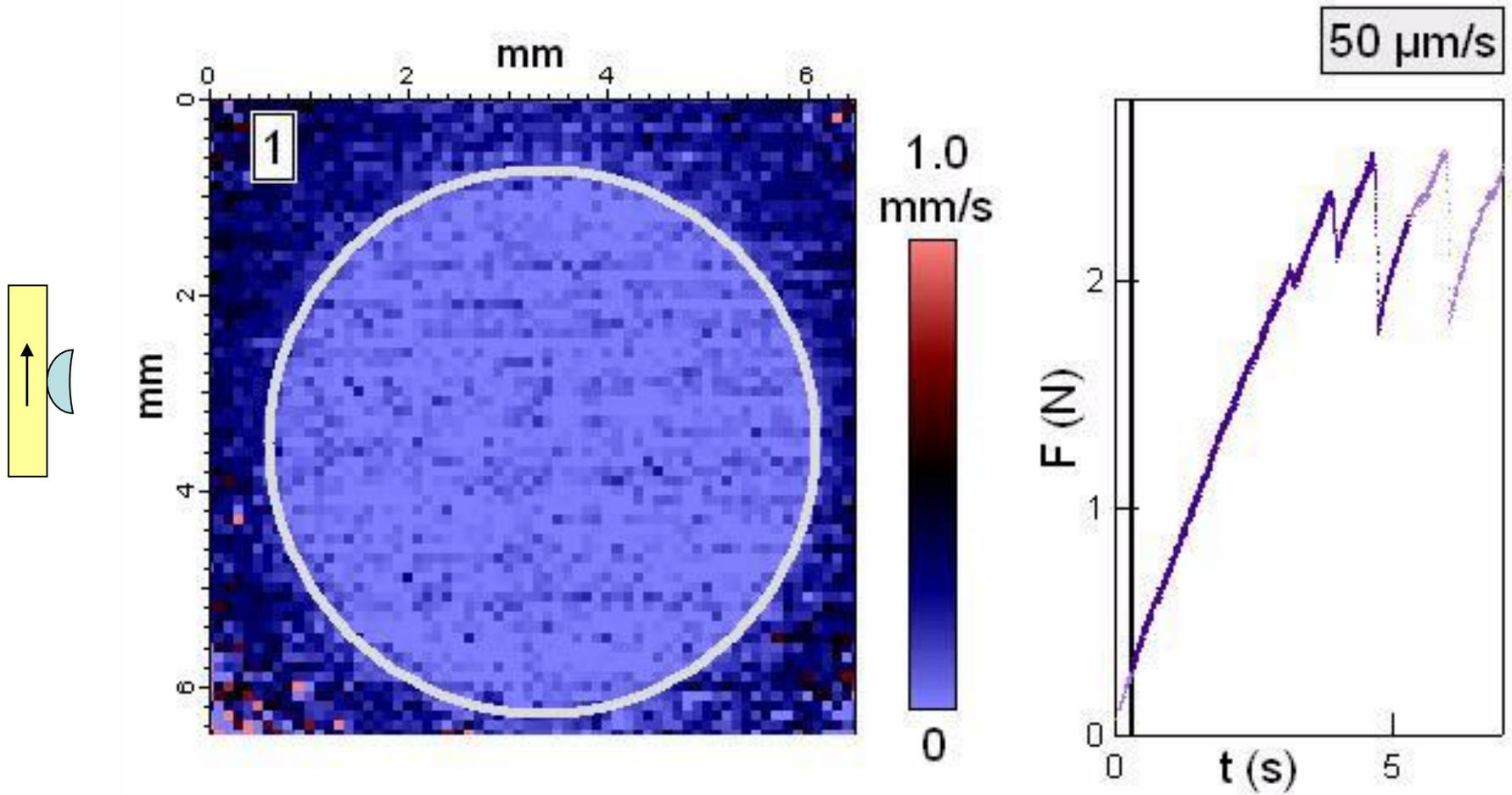
Friction traces : velocity dependence



Characteristic length: $\lambda = v/F \sim 70 \mu\text{m}$

Stiction with patterned lenses

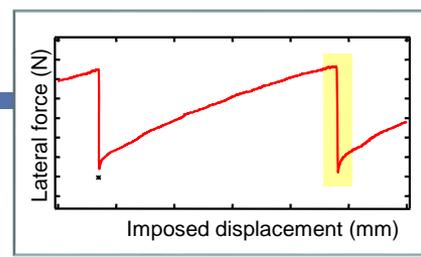
- Surface velocity field



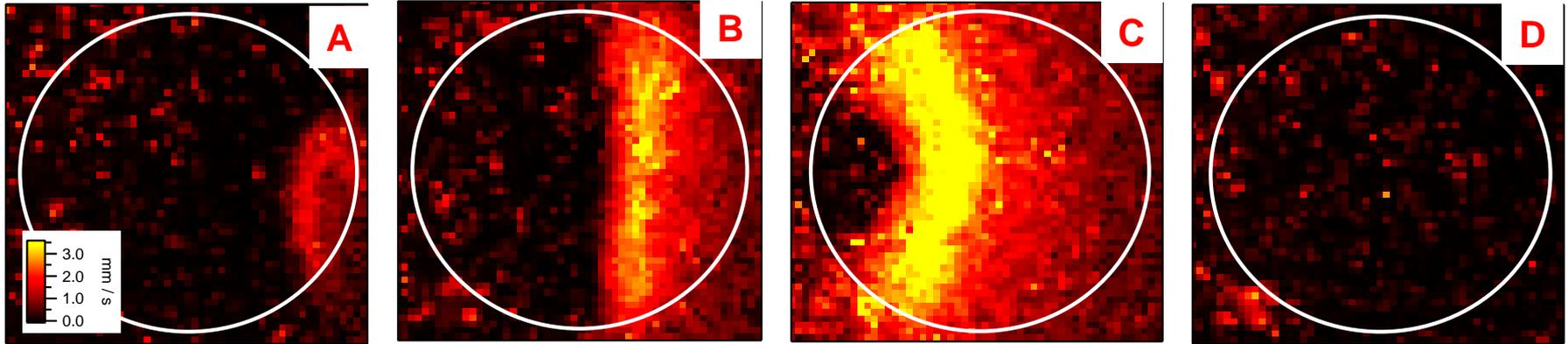
Crack-like precursors to friction

Established stick-slip regime : low velocity regime

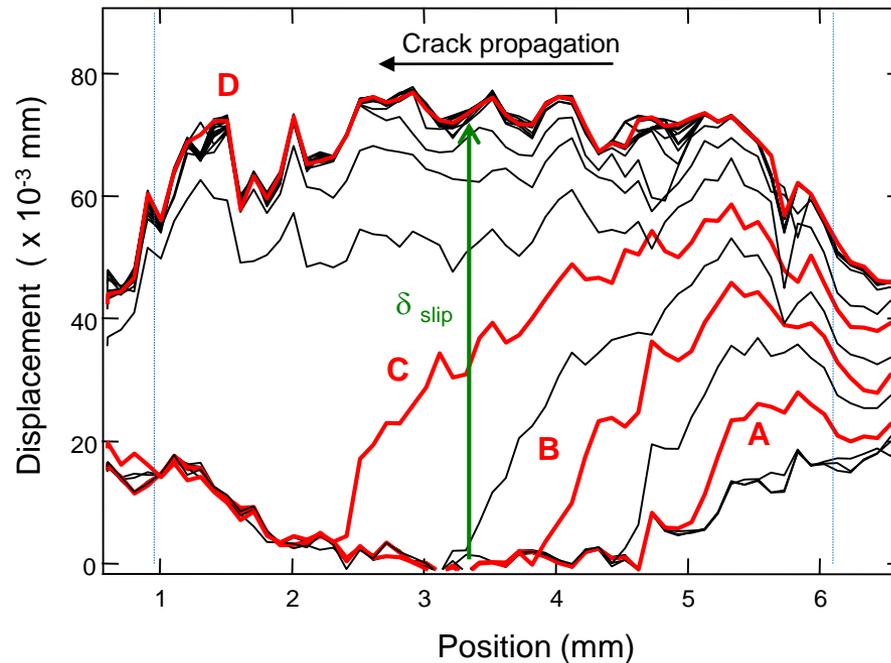
- 'Slip phase' - $v = 5 \mu\text{m s}^{-1}$



Slip velocity field

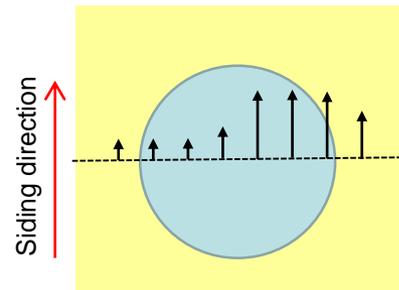


Displacement profile



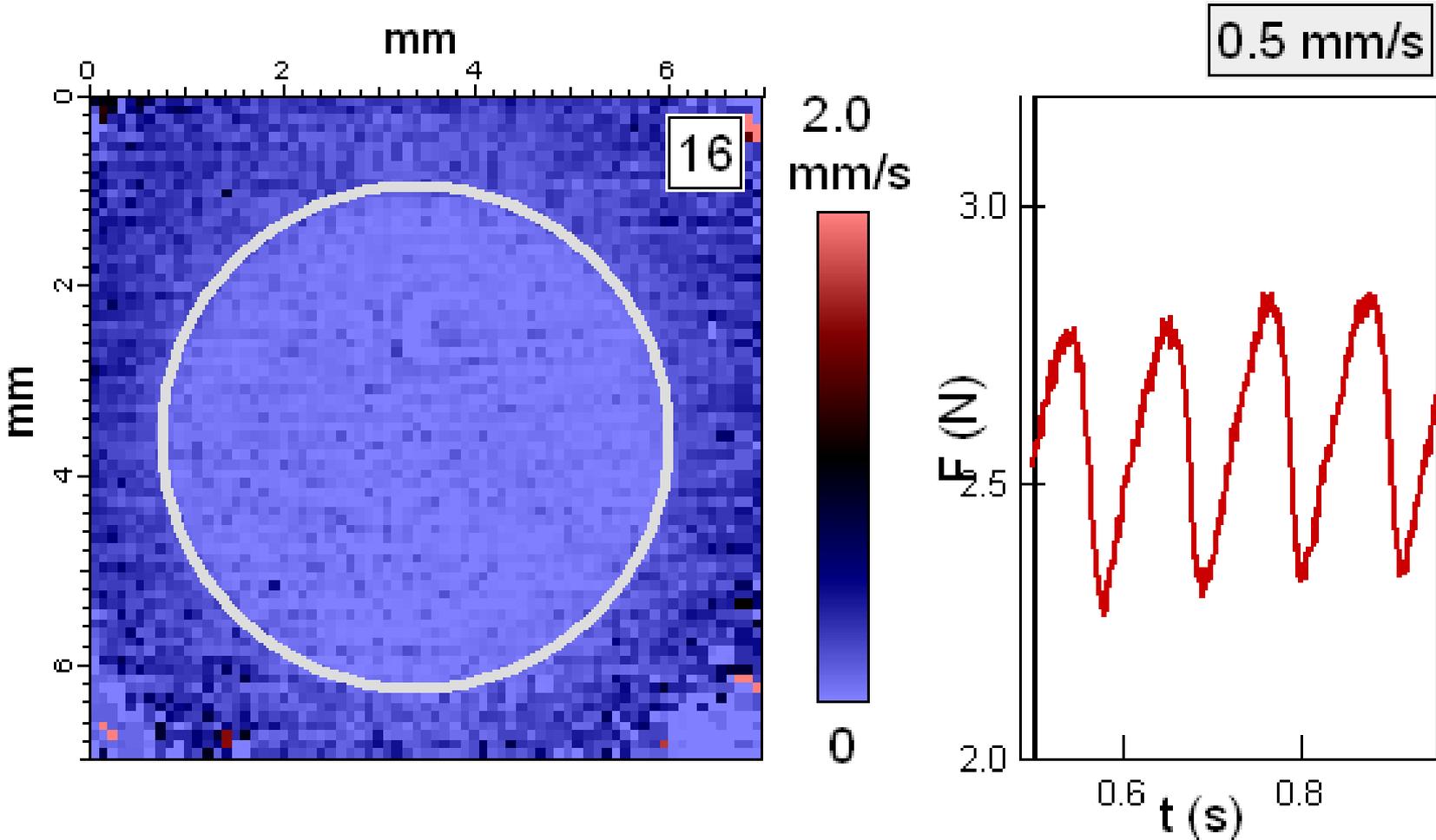
Crack velocity $\sim 100 \text{ mm s}^{-1}$

$\delta_{\text{slip}} \sim 70 \mu\text{m}$



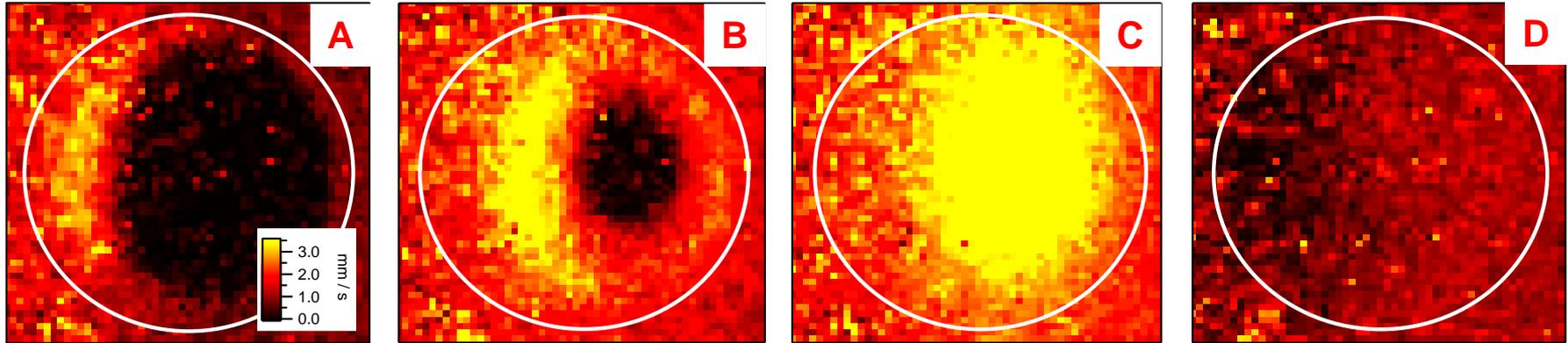
Established stick-slip regime : high velocity regime

- Surface velocity field - $v = 0.5 \text{ mm s}^{-1}$

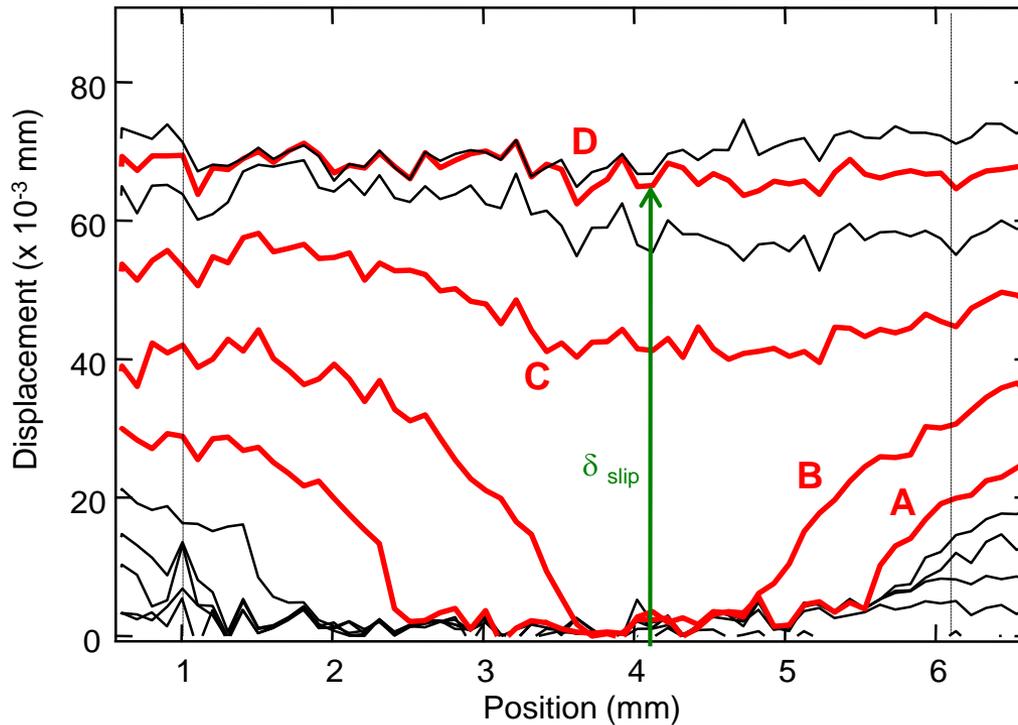


Stick slip regimes : high velocity

Slip velocity field



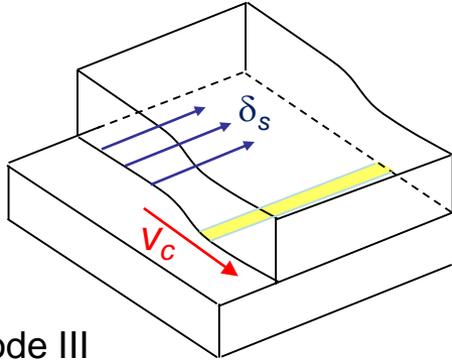
Displacement profile



Crack velocity ~ 100 mm s^{-1}

$\delta_{slip} \sim 70$ μm

Stick-slip as a crack-like motion



Mode III

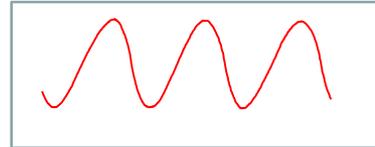
V_c & δ_s independent on the driving velocity

$$v < V_c < V_{Rayleigh}$$

- Typical propagation time: $t_p = 2a/v_c$

Low velocity: $t_p \ll T_{ss}$

High velocity: $t_p \approx T_{ss}$



- $\delta_s \approx cst$ → Stick slip frequency linearly related to the driving velocity $v = \delta_s/T_{ss}$

Parameters setting the slip length ?? How do the surfaces re-stick ??

- $V_c \approx cst$ → Fracture energy G_c ?

Threshold stress for crack nucleation \gg Threshold stress for quasi-static crack propagation

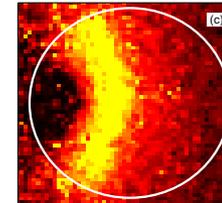
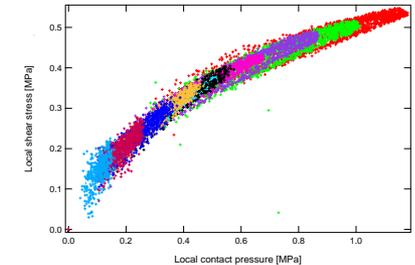
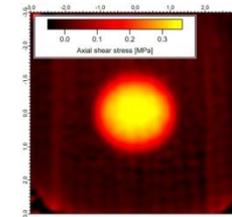
Reduced velocity dependence of G_c due to the interplay with friction ?

Conclusion /Outlook

- ✓ Local friction law from displacement field measurements
- ✓ Multi-contact interface with rigid randomly rough surface

Non linear local friction law
Relevance of spectral description of surface topography ?
Contribution of viscoelasticity to friction

- ✓ Crack-like precursors to friction during stick slip regime



Ongoing work: friction of model randomly rough surfaces

with A. Prevost and E. Wandersman, Paris Univ
M. Chaudhury, Lehigh University

Elastic coupling between micro-asperity contacts ?????

